

Class Nine Academic Program-2020

PHYSICS

Lecture : P-09

Chapter 4 : Work, Energy & Power

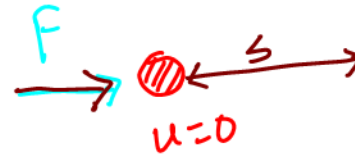


• Definition:

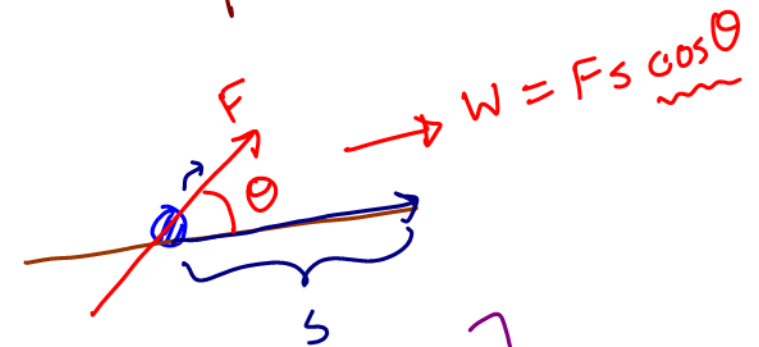
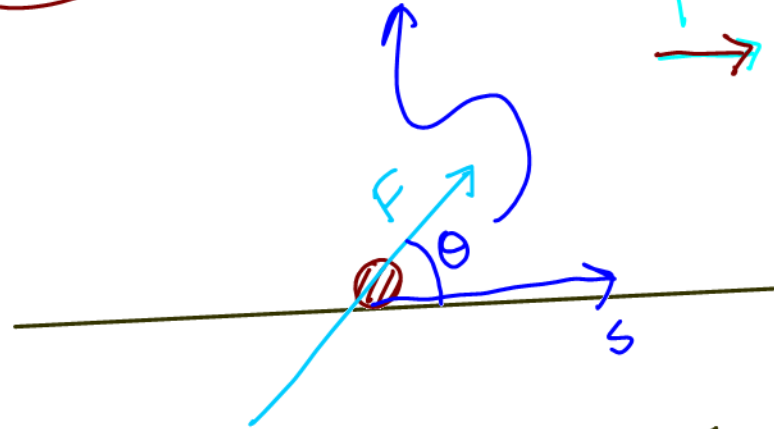
The product of applied force on an object and the displacement or the component of displacement towards the force during the application of force is known as Work.

$$W = Fs \quad / \quad Fs \cos \theta$$

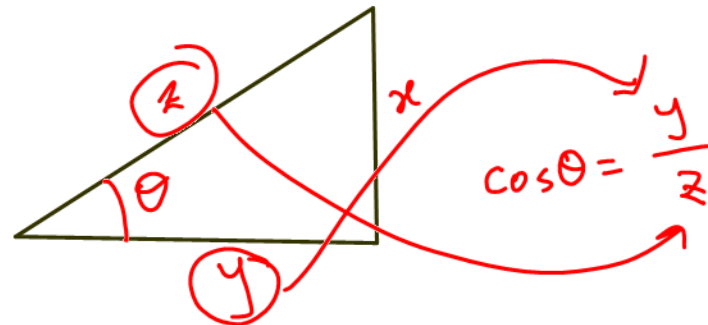
(i) → certain



(ii)



math



[কোণের দ্বারা] \cos \downarrow $\frac{y}{x}$ \downarrow $\frac{\text{Base}}{\text{Hypotenuse}}$

Work

✓ Work = Scalar;

$$W = \vec{F} \cdot \vec{s} \rightarrow \text{Dot Product} = F \cos \theta / F s$$

\swarrow vector \swarrow vector

Unit: J/Nm

Dimension: ✓

$$\rightarrow J \rightarrow Nm$$

$$\rightarrow Kgms^{-2}m$$

$$\rightarrow Kgm^2s^{-2}$$

So,

$$[W] = [M L^2 T^{-2}]$$

$$W = Fs$$

$\downarrow \quad \downarrow$
 $Nm \rightarrow J \text{ (Joule)}$

$$F = ma$$

$\downarrow \quad \downarrow$
 $kg \quad ms^{-2}$

$$\begin{aligned}
 &J \rightarrow Nm \\
 &\quad \downarrow \\
 &kgms^{-2}m \\
 &= kgm^2s^{-2} \\
 &\quad \downarrow \quad \downarrow \quad \downarrow \\
 &M \quad L \quad T^{-2}
 \end{aligned}$$

Problem

- 10N force is applied on an object for 5s and therefore displacement occurs 5m towards force. But, due to inertia of motion, the object moves 3m more. Work done =?

$$W = Fs$$

$$= (10 \times 5)$$

$$= 50 \text{ J}$$

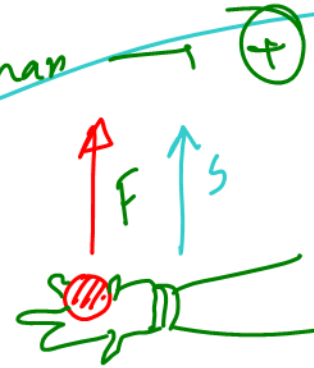
$$\begin{aligned} &\nearrow \text{a) } 50 \text{ J} \\ &\nearrow \text{b) } 80 \text{ J} \end{aligned}$$

Classification of Work

1. Positive Work:

→ Lift up a Pen. Your work.....

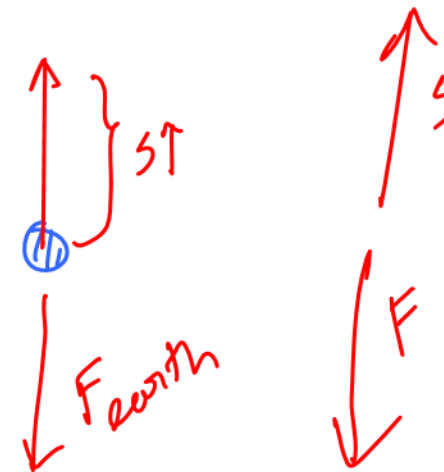
with respect to human



2. Negative Work:

→ Lift up a Pen. Earth's Work.....

with respect to earth



$$\begin{aligned} W &= Fs \cos \theta \\ &= Fs \cos 180^\circ \\ &= -Fs \\ &= -mgh \end{aligned}$$

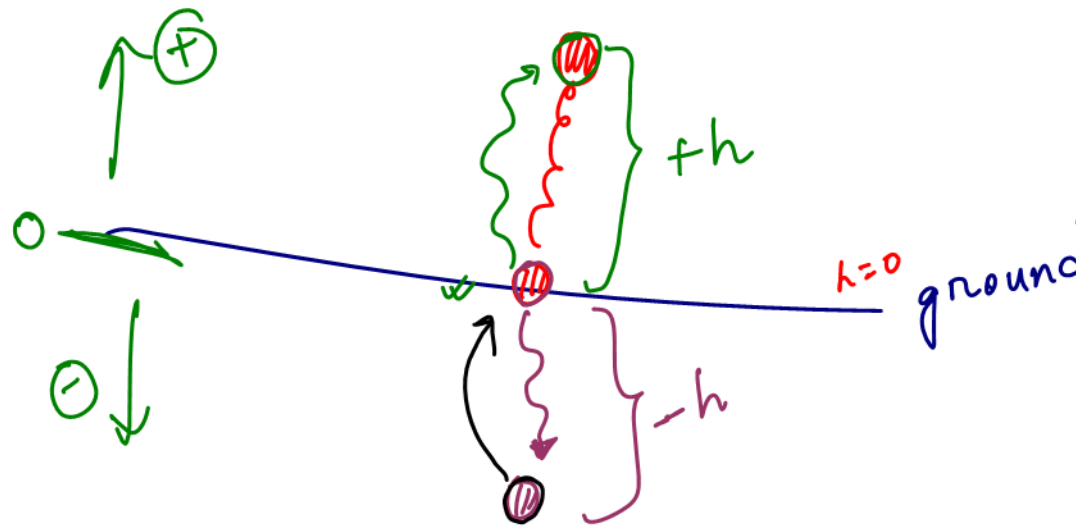
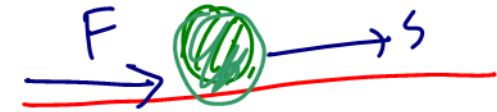
$F_{\text{earth}} = \text{Weight}$

Energy

(Ability to do work is called Energy.)

$$\text{Energy} = \text{Work (same)}$$

- ✓ During Positive Work → Giving Energy to the Object
- ✓ During Negative Work → Taking away Energy from the Object....



Energy

Work Done = Energy Created/ Released.

Unit: J/Nm

Dimension:

$$\rightarrow J \rightarrow Nm$$

$$\rightarrow Kgs^{-2}m$$

$$\rightarrow kgm^2s^{-2}$$

So,

$$[E] = [ML^2T^{-2}]$$

Different Forms of Energy

● Mechanical Energy :

(The energy that obtained due to Position, Shape & Motion of object is known as Mechanical Energy.)

Two Types:

→ Kinetic Energy

→ Potential Energy

Kinetic Energy

****The Energy due to Motion is called Kinetic Energy.**

We Know,

Energy released / created = Work Done

So,

$$E_k = W = Fs$$

$$E_k = mas \dots (i)$$

But,

$$v^2 = u^2 + 2as$$

$$\Rightarrow v^2 = 2as \quad [\because u = 0]$$

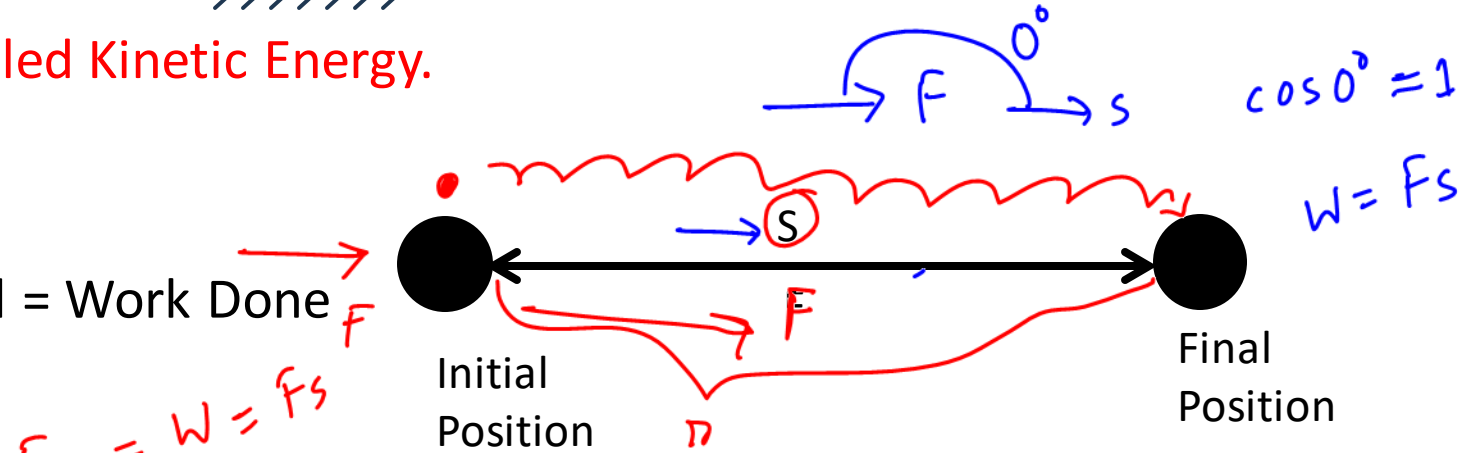
$$\Rightarrow as = \frac{v^2}{2}$$

$$\therefore (i) \Rightarrow$$

$$E_k = m \times \left(\frac{v^2}{2} \right) = \frac{1}{2}mv^2$$

momentum

$$E_k = P^2 / 2m ?$$



$$E_k = \frac{1}{2}mv^2$$

$$E_k = \frac{1}{2}mv^2$$

$$= \frac{1}{2} \frac{m^2 v^2}{m} = \frac{1}{2} \frac{(mv)^2}{m}$$

$$E_k = \frac{1}{2} \frac{P^2}{m}$$

$$E_k = \frac{P^2}{2m}$$

Poll -01

- If the momentum of an object becomes 2 times, then the kinetic energy will be:

- A) 4 times ✓
- B) 2 times
- C) 1.41 times
- D) 8 times

$$E_k = \frac{p^2}{2m}$$

$E_k \propto p^2$

2 times

?

$E_k \propto p^2$

$2^2 = 4$

9

$E_k \propto p^2$

2

9 times

$E_k \propto 2^2 = 4$

$p \rightarrow 2 \text{ times}$

$p \rightarrow 2 \text{ times}$

$p^2 \rightarrow 2^2 = 4$

Work-Energy Theorem

We Know,

$$v^2 = u^2 + 2as$$

Multiplying both sides by $\frac{1}{2}m \Rightarrow$

$$\Rightarrow \frac{1}{2}mv^2 = \frac{1}{2}mu^2 + \frac{1}{2}m \times 2as$$

$$\Rightarrow \frac{1}{2}mv^2 - \frac{1}{2}mu^2 = mas = Fs$$

$$\Rightarrow \frac{1}{2}mv^2 - \frac{1}{2}mu^2 = W$$

Work –Energy Theorem.

$$\begin{aligned} \frac{1}{2}mv^2 &= \frac{1}{2}mu^2 + \frac{1}{2}m \times 2as \\ &= \frac{1}{2}mu^2 + mas \\ &= \frac{1}{2}mu^2 + Fs \\ &= W \end{aligned}$$

Problem

● A force of 10N is applied on a stationary object of mass 10kg for 10s.

a) Calculate the kinetic energy after 10s.

b) Calculate the kinetic energy after 20s.

c) Calculate the kinetic energy if Force is applied for total 20s.

a) After 10s, $E_k = \frac{1}{2}mv^2$

$$\rightarrow v = u + at$$

$$= 0 + at$$

$$\Rightarrow v = at$$

$$\Rightarrow v = a \times 10 = 10a$$

$$= 10 \times 1$$

$$= 10 \text{ m/s}$$

$$a = \frac{F}{m} \quad [F = ma]$$

$$= \frac{10}{10} = 1 \text{ m/s}^2$$

$$E_k = \frac{1}{2} \times m \times v^2$$

$$= \frac{1}{2} \times 10 \times (10)^2$$

$$= \frac{1}{2} \times 10 \times 100$$

$$= 500 \text{ J} \cdot \text{Ans}$$

b) ~~500 J / 1000 J~~

10s time → Force applied



উদ্ভাস

একাডেমিক এন্ড এডমিশন কেয়ার

Solution

$$c) a = 1 \text{ m s}^{-2}$$

$$t = 20 \text{ sec}$$

$$\Rightarrow v = u + at$$

$$\Rightarrow v = 0 + 1 \times 20$$

$$\Rightarrow v = 20 \text{ m/s}$$

$$\Rightarrow E_k = \frac{1}{2} mv^2$$

$$= \frac{1}{2} \times 10 \times (20)^2 \text{ J}$$

$$= \frac{1}{2} \times 10 \times 400 \text{ J}$$

$$= 2000 \text{ J} . \underline{\text{Ans.}}$$

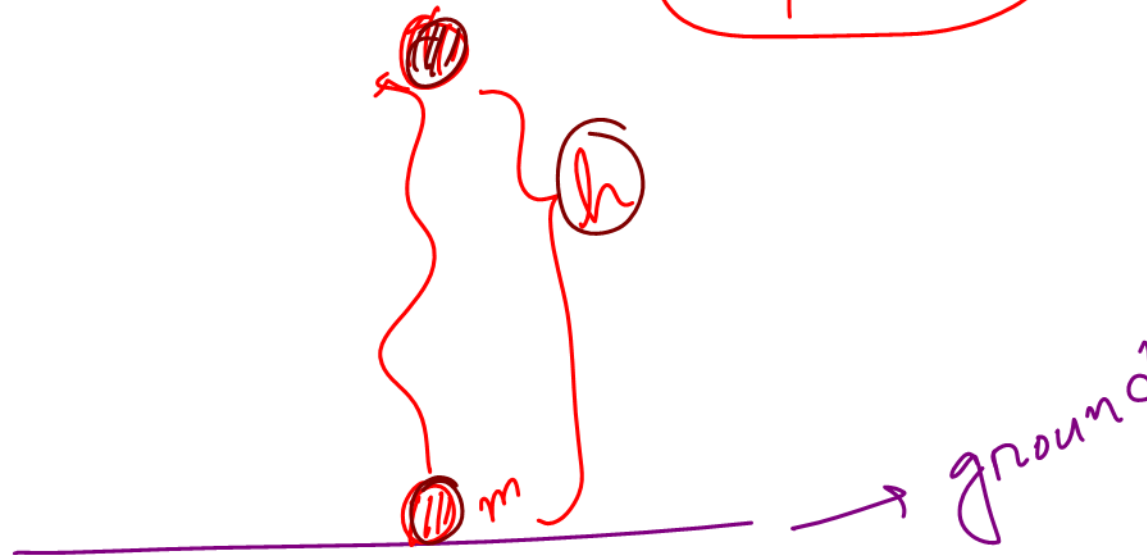
Potential Energy

****The energy that happens due to change of position & shape of an object, is called potential energy.**

Suppose, an object mass of 'm' is placed on a building of 'h' height. Then, due to change of position, the potential energy, $E_p = mgh$

$$\begin{aligned}
 E_p &= W \\
 &= F \cdot s \\
 &= mgh \\
 E_p &= mgh
 \end{aligned}$$

$$E_p = mgh$$



Quiz

Can Kinetic Energy be negative? →

$$E_k = \frac{1}{2}mv^2$$

$$E_p = mgh$$

↓
From ground

positive

No

$$E_k = \frac{1}{2}mv^2$$

mass
kg

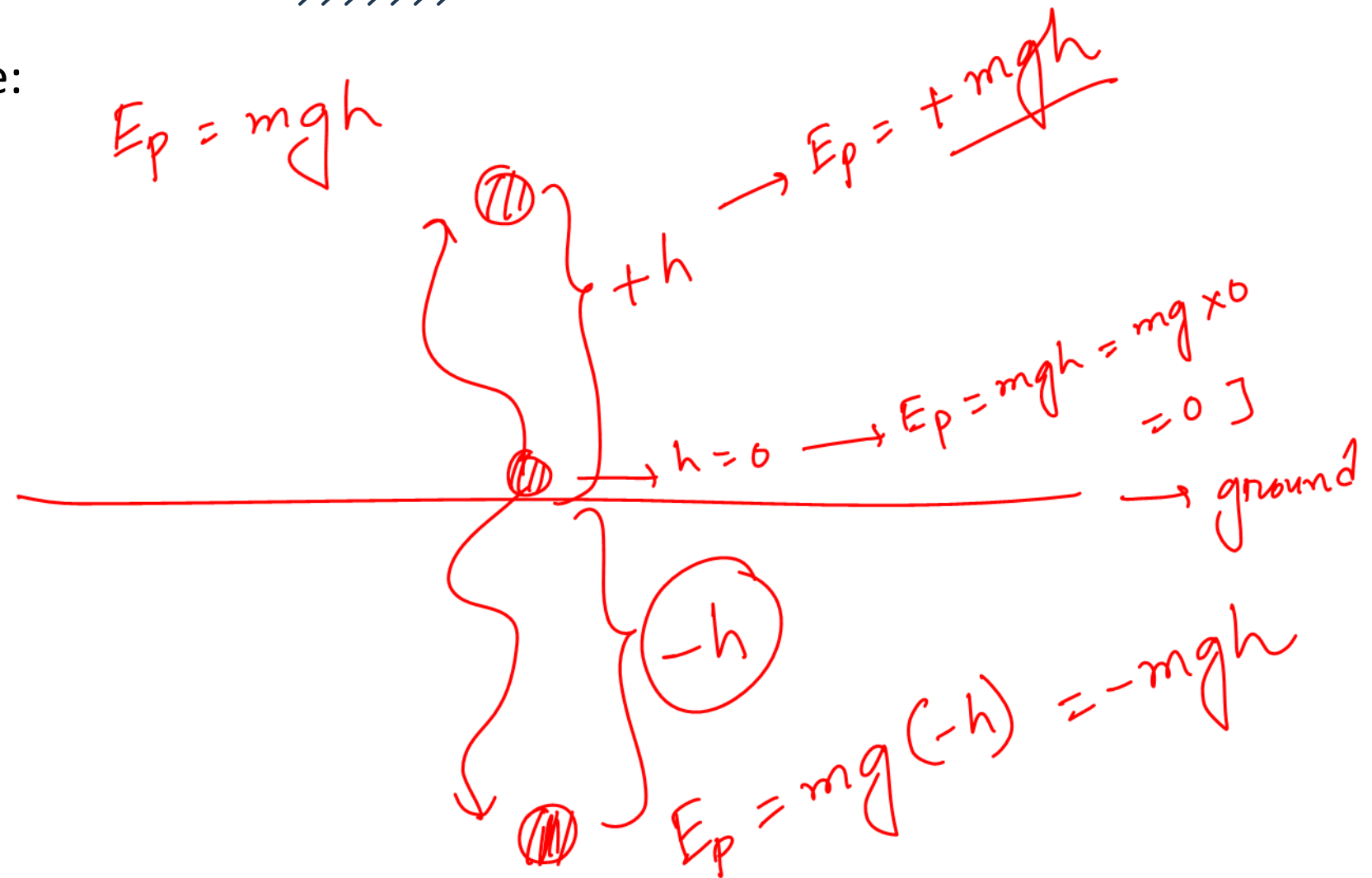
✓

$(-5)^2 = 25$

• Potential energy can be:

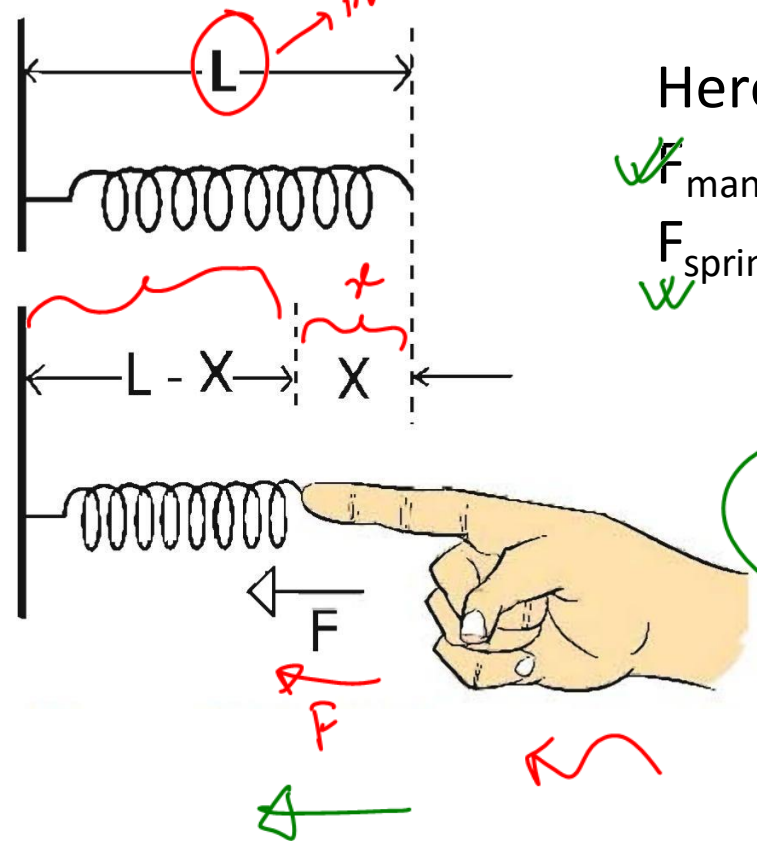
- A) Positive
- B) Negative
- C) 0
- ~~D) All~~

$$E_p = mgh$$



Spring

- For a spring, Potential Energy, $E_p = \frac{1}{2} Kx^2$; K = Spring Constant, x = Expansion / Compression.

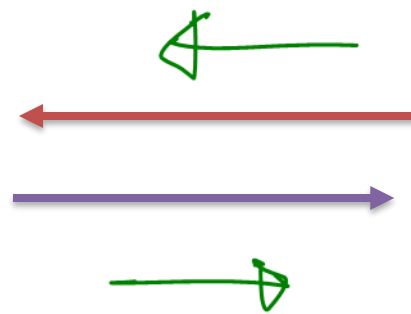


Here,
 F_{man} = Human
 F_{spring} = Spring

$$E_p = \frac{1}{2} Kx^2$$

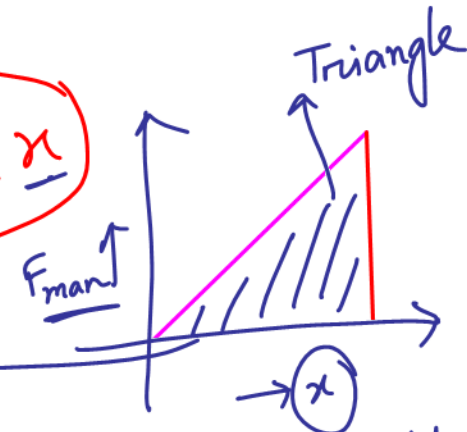
$$= \frac{1}{2} \times x \times Kx$$

$$E_p = \frac{1}{2} Kx^2$$



$$F_{man} = Kx$$

$$\Rightarrow F_{man} \propto x$$

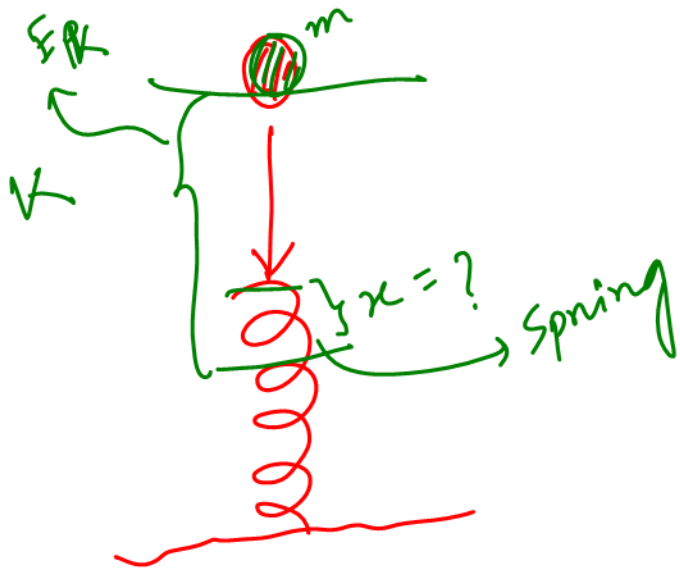


Area of triangle = $\frac{1}{2} \times \text{base} \times \text{height}$

$$= \frac{1}{2} \times x \times F_{man}$$

Law of Conservation of Energy

Q ✓ A body of mass 10kg fell on a spring with a velocity of 10 m/s. If Spring Constant = 100000 J/m² or N/m, what was the compression of the spring?



$$E_k = E_p$$

$$\Rightarrow \frac{1}{2}mv^2 = \frac{1}{2}kx^2$$

$$\Rightarrow mv^2 = kx^2$$

$$\Rightarrow x^2 = \frac{mv^2}{k}$$

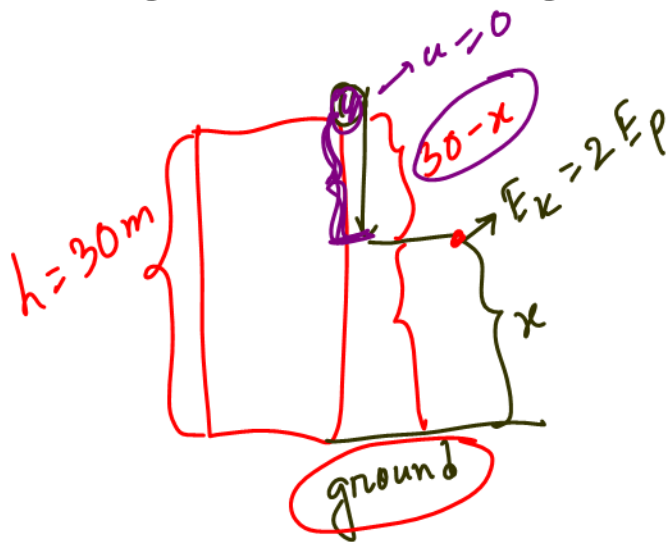
$$\Rightarrow x = \sqrt{\frac{mv^2}{k}}$$

Handwritten calculations in red ink: 10 (for v), $(10)^2$ (for v^2), and 100000 (for k).

$$\Rightarrow x = 0.1 \text{ m}$$

Problem

Q. At which height does Kinetic Energy become 2 times of Potential Energy if the object falling from 30m height?



Let, x m height from ground.

$$E_p = mgh \text{ (from ground)}$$

$$= mg \times x$$

$$\Rightarrow E_p = mgx$$

$$E_k = \frac{1}{2}mv^2$$

$$= \frac{1}{2}m(u^2 + 2gh)$$

$$= \frac{1}{2}m \times 2gh$$

$$= \frac{1}{2} \times m \times 2g(30-x)$$

$$= \frac{1}{2}m \times 2g(30-x)$$

$$E_k = mg \times 30 - mgx$$

Solution

According to Ques \Rightarrow

$$E_k = 2 E_p$$

$$\Rightarrow mg30 - mgx = 2(mgx)$$

$$\Rightarrow mg30 - mgx = 2mgx$$

$$\therefore mg30 = 3mgx$$

$$\Rightarrow x = \frac{30}{3} = \textcircled{10\text{m}}. \text{ (From ground)}$$

Shortcut♥♥

$$E_k = 2E_p \rightarrow n$$

Here, **n** means how many times will be Kinetic Energy of Potential Energy

$$\text{Shortcut} \Rightarrow x = \frac{h}{n+1}$$

$$E_k = n E_p$$

* If $E_p = 2E_k \Rightarrow$
 $E_k = \frac{1}{2} E_p \rightarrow n$

$$x = \frac{h}{\frac{1}{2} + 1}$$

$$x = \frac{h}{n+1} = \frac{30m}{2+1} = \frac{30}{3} = 10m$$

$$E_k = 2E_p$$

$$E_k = 4E_p \rightarrow n=4$$

না বুঝে মুখস্থ করার অভ্যাস
প্রতিভাকে ধ্বংস করে।



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