

بِسْمِ اللَّهِ الرَّحْمَنِ الرَّحِيمِ

বিস্মিল্লাহির রাহমানির রাহীম



কুন্দন

একাডেমিক এন্ড এডমিশন কেয়ার

দশম শ্রেণি: সা.গণিত (অধ্যায়-৮)

বৃত্ত
লেকচার : M-21

Poll 1

Length of the perpendicular drawn on the hypotenuse (from the vertex opposite to the hypotenuse) can't be greater than half of the hypotenuse.

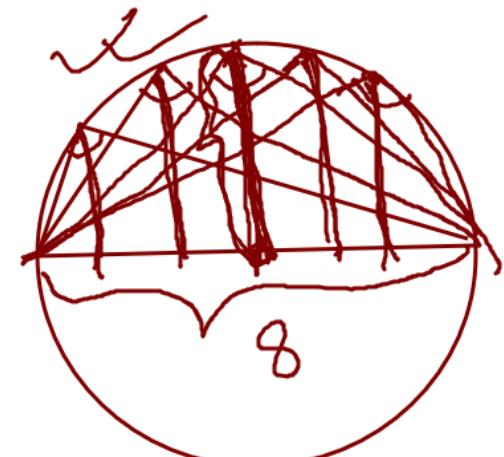
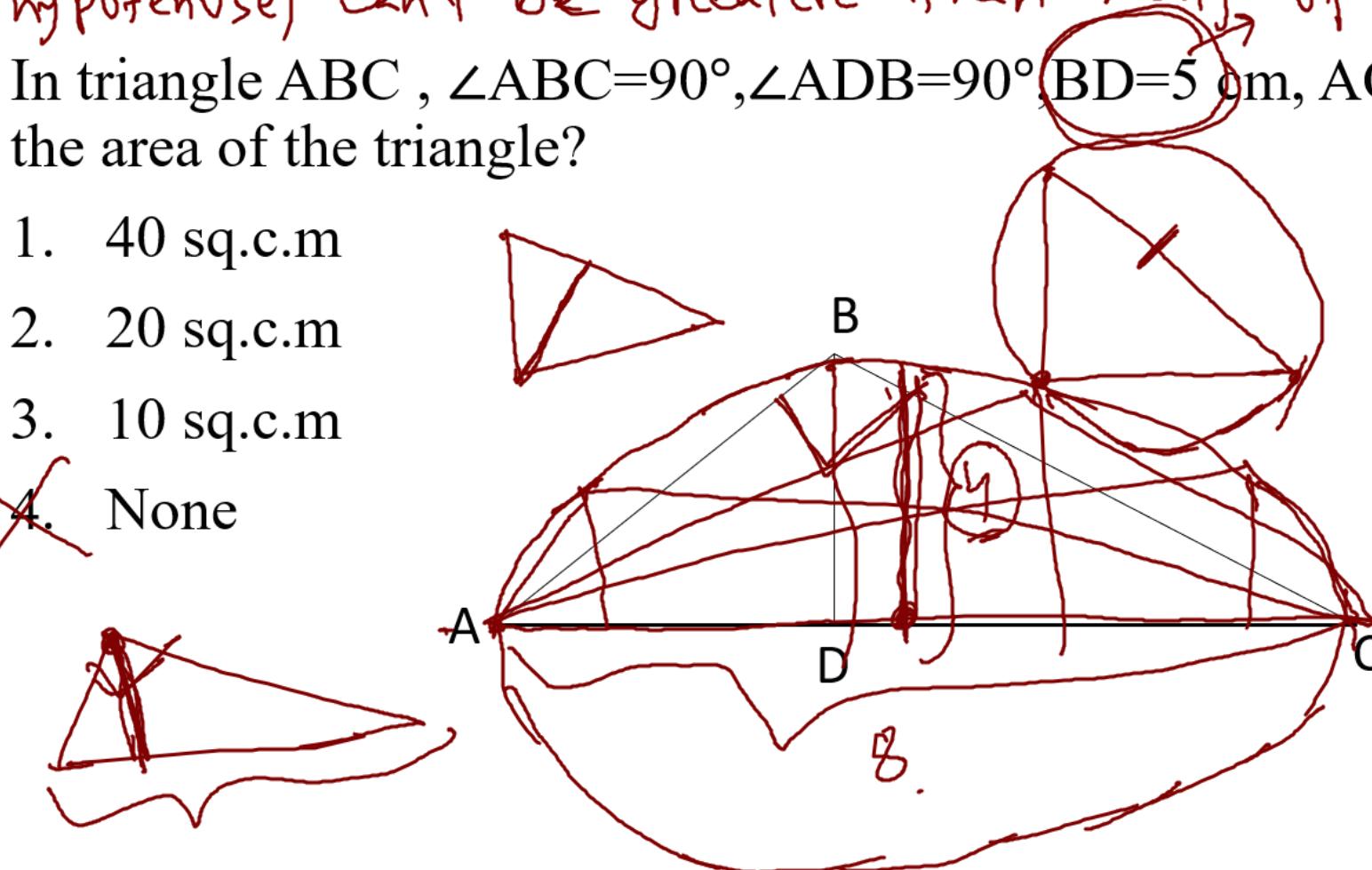
In triangle ABC , $\angle ABC=90^\circ$, $\angle ADB=90^\circ$, $BD=5 \text{ cm}$, $AC=\underline{8} \text{ cm}$. What is the area of the triangle?

1. 40 sq.c.m

2. 20 sq.c.m

3. 10 sq.c.m

~~4.~~ None



Poll 2

What is the area of a triangle having sides' length of 2 cm, 3 cm and 6 cm ?

1. 9 sq.c.m
2. 18 sq.c.m
3. 11 sq.cm
4. None

$$2 + 3 = 5$$

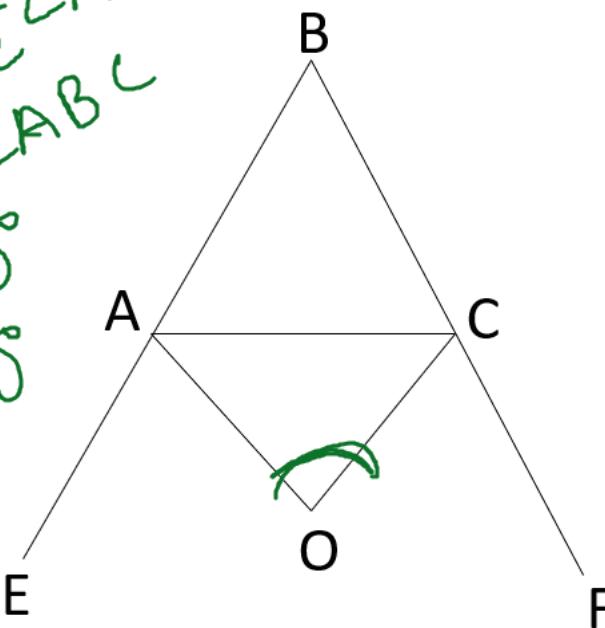
$$5 < 6,$$

Poll 3

OA and OC are bisectors of $\angle EAC$ and $\angle FCA$ respectively. If $\angle AOC=50^\circ$, then $\angle ABC=?$

1. 40
2. 130
3. 25
4. 80

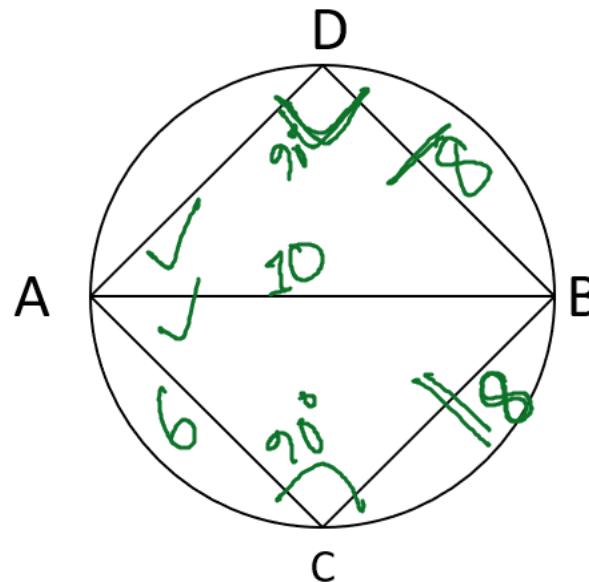
$$\begin{aligned}\angle AOC &= 90^\circ - \frac{1}{2} \angle ABC \\ 50^\circ &= 90^\circ - \frac{1}{2} \angle ABC \\ \frac{1}{2} \angle ABC &= 40^\circ \\ \angle ABC &= 80^\circ\end{aligned}$$



Poll 4

Here ADBC is an inscribed quadrilateral and AB is the diameter of the circle. $\angle \text{BAD} = \angle \text{BAC}$. If $\text{AC} = 6\text{cm}$, $\text{AB} = 10\text{cm}$. $\text{BD} = ? \text{ cm}$

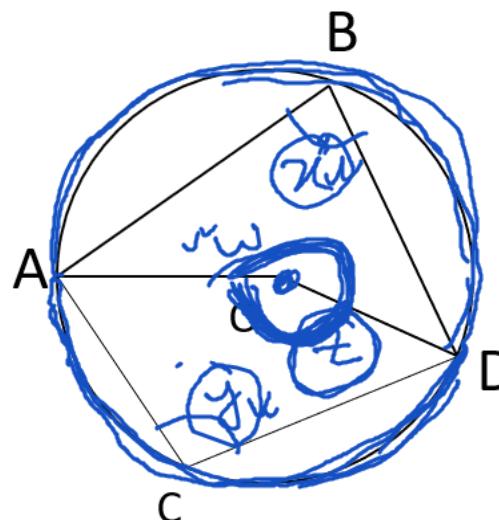
- 1. 8
- 2. 9
- 3. 4.5
- 4. 5



$$\sqrt{10^2 - 6^2} = 8$$

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The sum of the two opposite angles of a inscribed quadrilateral is two right angles.



$$2x = z$$

$$2y = w$$

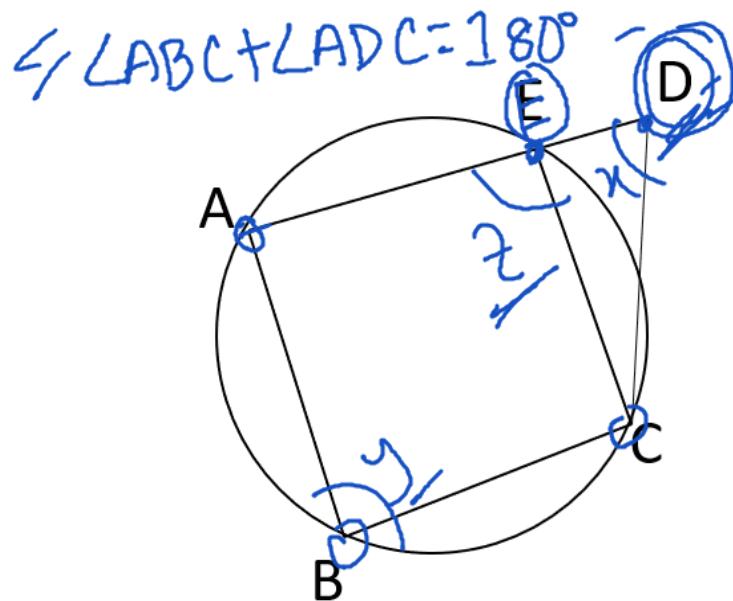
$$2(x+y) = w+z$$

$$2(x+y) = 360^\circ$$

$$w+z = 180^\circ$$

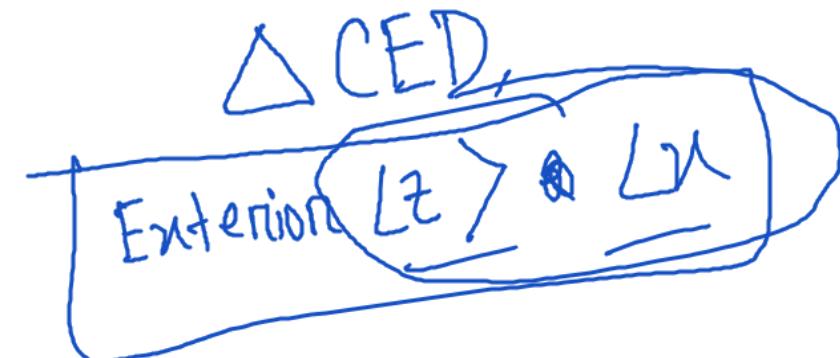
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If two opposite angles of a quadrilateral are supplementary, then the four vertices of the quadrilateral are concyclic.

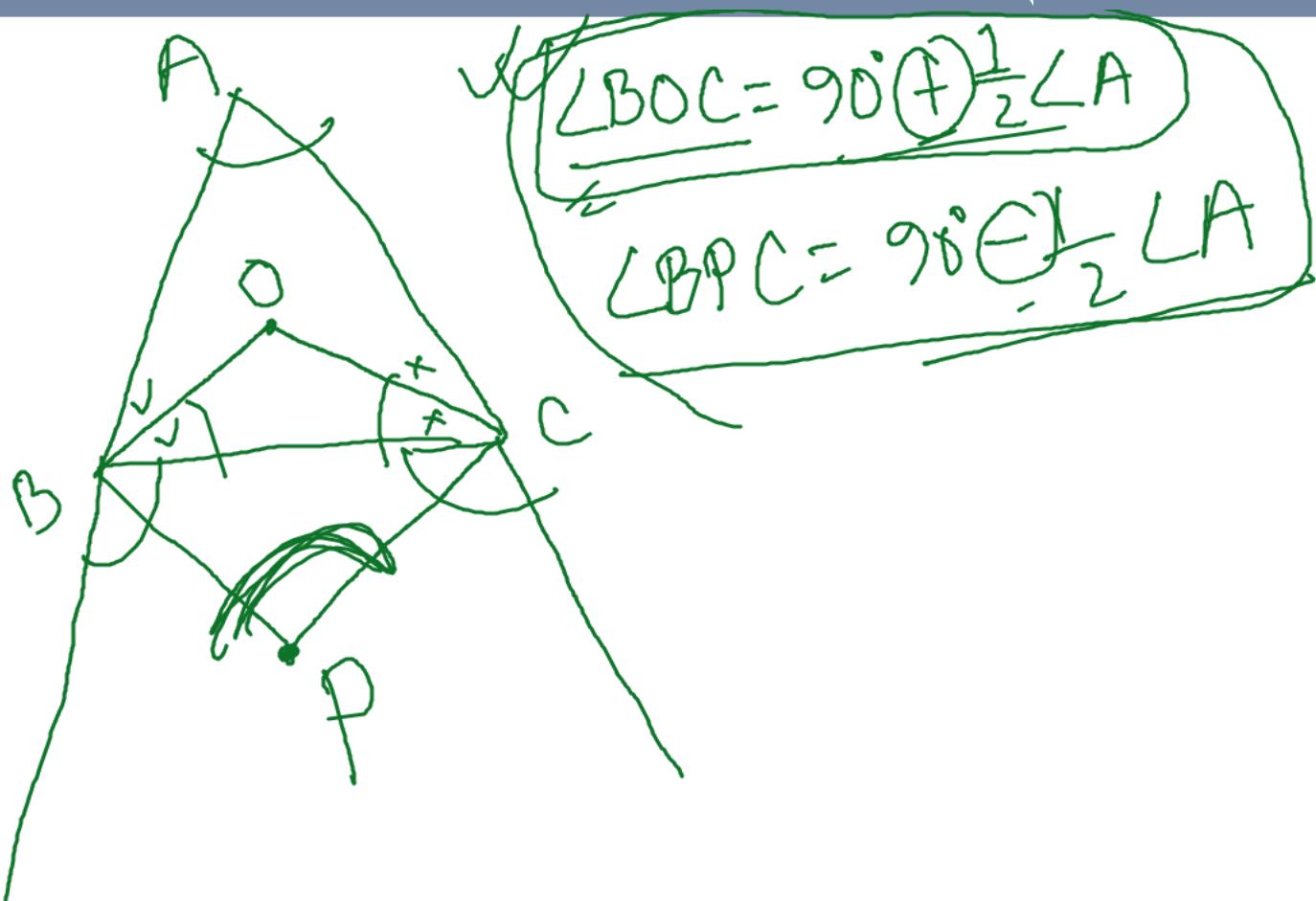


method of contradiction

$$\begin{aligned} x+y &= 180^\circ \\ y+z &= 180^\circ \\ x+y &= y+z \\ x &= z \end{aligned}$$



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$$\angle A + \angle B + \angle C = 180^\circ$$

$$\frac{1}{2} \angle A + \frac{1}{2} \angle B + \frac{1}{2} \angle C = 90^\circ$$

$$\frac{1}{2} \angle A + \angle OBC + \angle OCB = 90^\circ$$

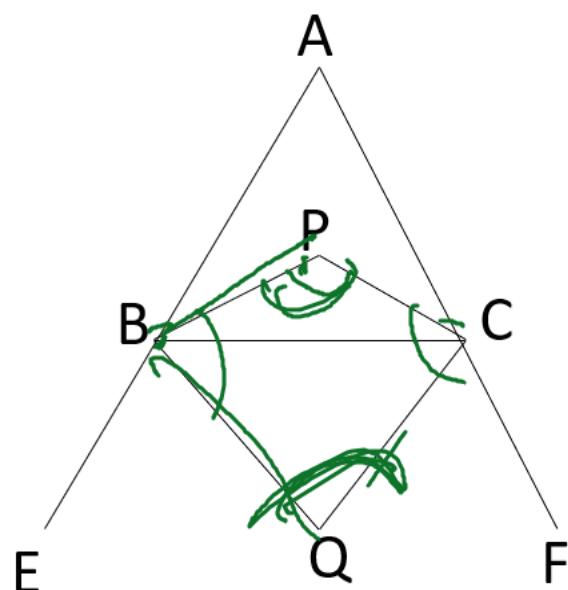
$$\underline{\angle BOC} + \underline{\frac{1}{2} \angle A} + \underline{\angle OBC} + \underline{\angle OCB} = 90^\circ + \underline{\angle BOC}$$

$$180^\circ + \frac{1}{2} \angle A = 90^\circ + \angle BOC$$

$$90^\circ + \frac{1}{2} \angle A = \angle BOC$$

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1. If the internal and external bisectors of the angles $\angle B$ and $\angle C$ of triangle ABC meet at points P and Q respectively, then prove that B,P,C,Q are concyclic.



$$\angle BPC = 90^\circ + \frac{1}{2} \angle A$$

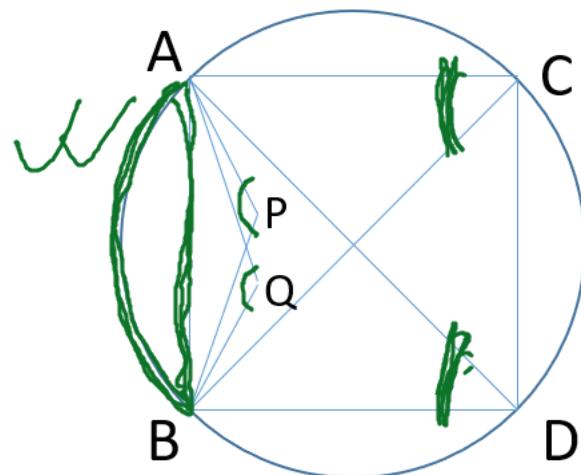
$$\angle BQC = 90^\circ - \frac{1}{2} \angle A$$

$$\angle BPC + \angle BQC = 180^\circ$$

$\therefore B, P, C, Q$ are concyclic.

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2. ABDC is an inscribed quadrilateral. If the bisectors of $\angle CAB$ and $\angle CBA$ meet at the point P and the bisectors of $\angle DBA$ and $\angle DAB$ meet at point Q , then prove that, the four points A,P,Q,B are concyclic.



$$\angle APB = 90^\circ + \frac{1}{2} \angle ACB$$

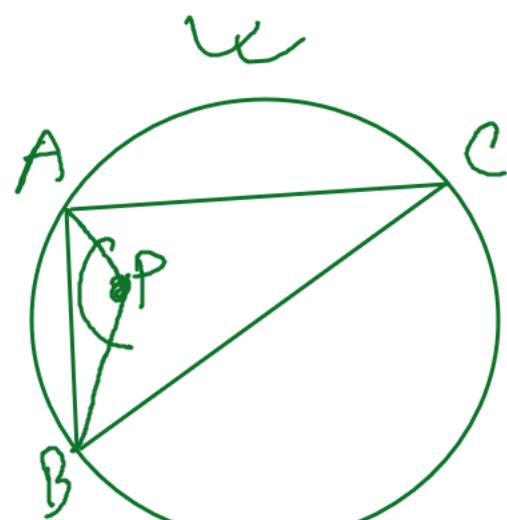
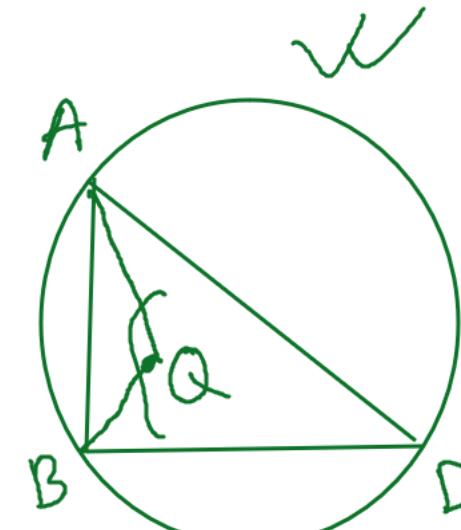
$$\therefore \angle APB = 90^\circ + \frac{1}{2} \angle ADB$$

$$\angle AQB = 90^\circ + \frac{1}{2} \angle ADB$$

$$\therefore \underline{\angle APB = \angle AQB}$$

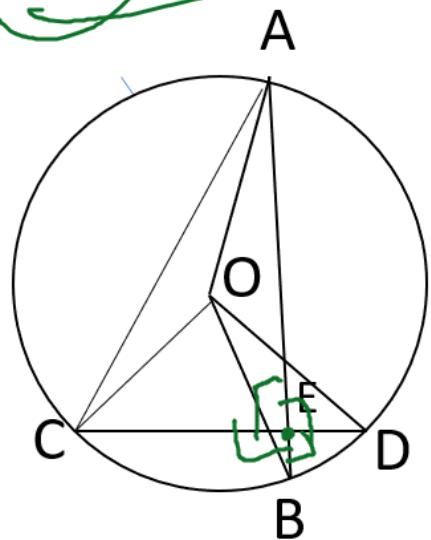
~~$$\angle ACB = \angle ADB$$~~

A,P,Q,B are
concylic



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3. The chords AB and CD of a circle with center O meet at right angles at any point inside the circle, prove that $\angle AOD + \angle BOC = 2$ right angles.



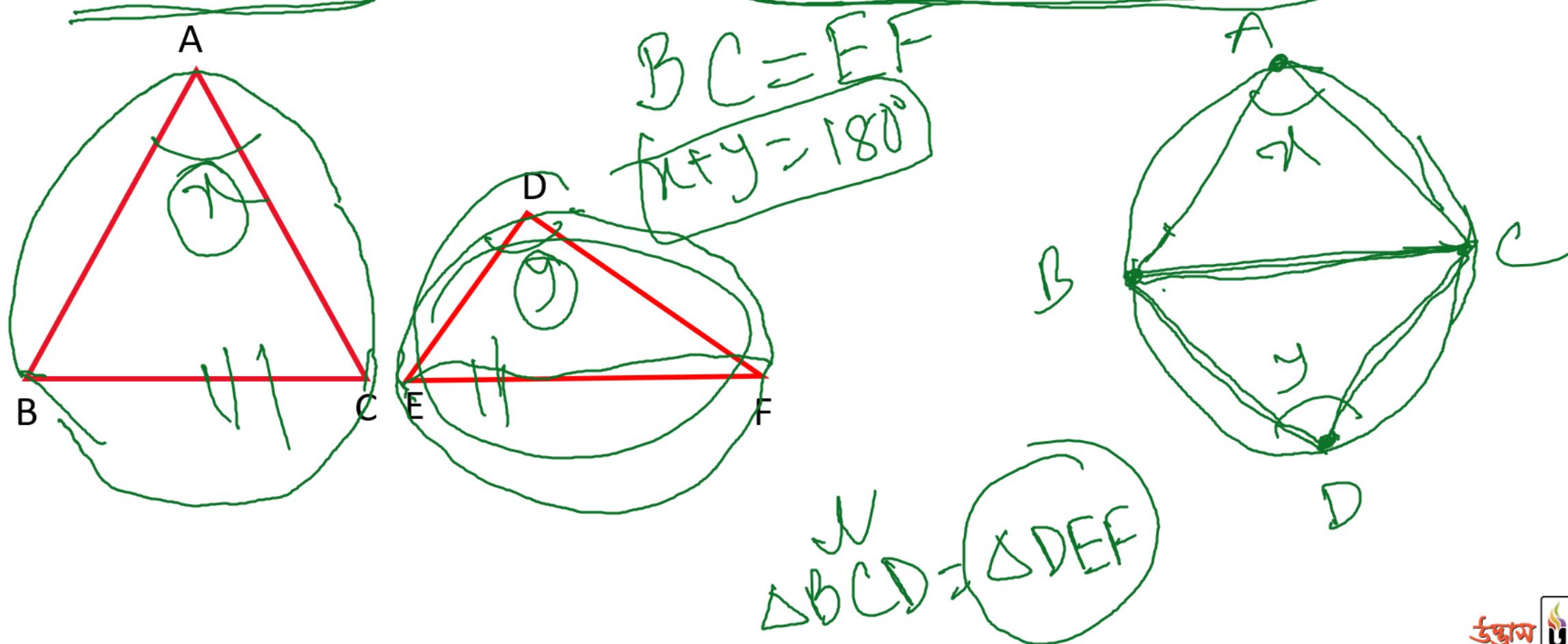
8.2 → (1)

$$2\angle AEC \\ 2 \times 90^\circ = 180^\circ$$

$$\angle AEC = \angle AED = \angle BEC = \angle BED = 90^\circ$$

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6. If the vertical angles of two triangles standing on equal bases are supplementary, then prove that their circum-circles are equal.



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ସ୍ଵପ୍ନ ଜୟ ତୋମାରି ହବେ

ଡକ୍ଟ୍ରାମ-ଉନ୍ନୟଷ୍ଠ ଶିକ୍ଷା ପରିବାର